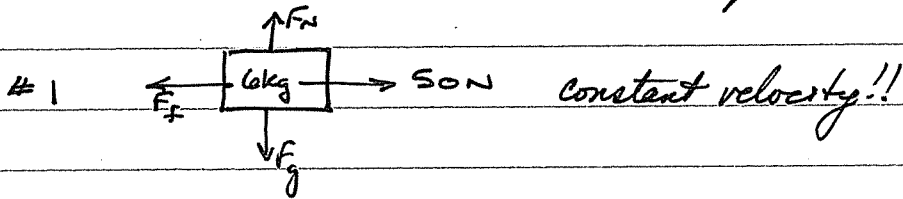


Friction, Newton's Laws + Kinematics



(a) $F_a = 50\text{ N}$

(d) $F_N = 58.8\text{ N} \quad \because F_{\text{Net}} = 0\text{ N VERT.}$

(b) $F_f = 50\text{ N} \quad \because F_{\text{Net}} = 0\text{ N}$

(c) $F_g = mg$
 $= 6(9.8)$
 $= 58.8\text{ N}$

(e) $F_f = \mu F_N$
 $50 = \mu 58.8$
 $\mu = 0.85$

(f) μ_k
 \because object
 is moving

#2 $\mu_k = 0.35$

$m = 5.0\text{ kg}$

$F_f = ?$

$F_N = F_g = mg$
 $= 5(9.8)$
 $= 49\text{ N}$

$F_f = \mu_k F_N$
 $= 0.35(49)$
 $= 17.2\text{ N}$

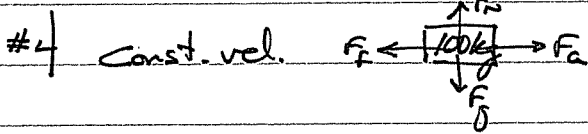
#3 $m = 70\text{ kg}$

$\mu = 0.010$

$F_f = ?$

$F_N = F_g = mg$
 $= 70(9.8)$
 $= 686\text{ N}$

$F_f = \mu_k F_N$
 $= 0.01(686)$
 $= 6.86\text{ N}$

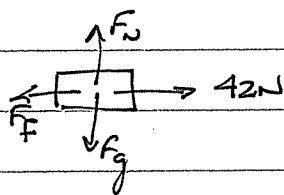


$F_a = F_f = 880\text{ N}$

$\therefore F_{\text{Net}} = 0$

$F_f = \mu F_N$
 $880 = \mu(mg)$
 $880 = \mu(100 \cdot 9.8)$
 $\mu = 0.898$

#5



$$F_f = 42 \text{ N} \quad \therefore F_{\text{NET}} = 0 \text{ N}$$

$$m = 5.0 \text{ kg}$$

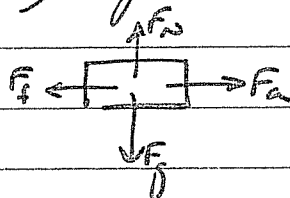
$$\mu = ?$$

$$F_f = \mu F_N$$

$$42 = \mu (mg)$$

$$\mu = 0.857$$

#6 uniform vel. !!



$$F_f = F_a = 180.3 \text{ N} \quad \therefore F_{\text{NET}} = 0 \text{ N}$$

$$\mu = 0.20$$

$$m F_g = ?$$

$$F_N = mg$$

$$F_f = \mu F_N$$

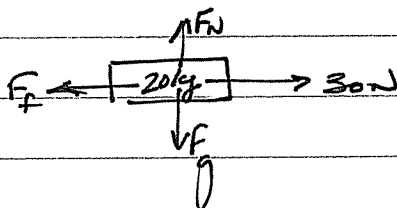
$$180.3 = 0.2 (mg)$$

$$901.5 = mg$$

$$m = 901.5 / 9.8$$

$$= 92 \text{ kg}$$

#7



$$(a) m = 20 \text{ kg}$$

$$F_a = 30 \text{ N}$$

$$\therefore F_f = 30 \text{ N} \text{ assuming unif. vel.}$$

$$\mu = ?$$

$$F_f = \mu F_N$$

$$30 = \mu (mg)$$

$$30 = \mu (20 \cdot 9.8)$$

$$\mu = 0.153$$

$$(b) m = 20 + 2(60) = 140 \text{ kg}$$

$$F_a = ?$$

→ assuming unif. velocity

$$F_a = F_f = \mu F_N$$

$$= 0.153 (140 \cdot 9.8)$$

$$= 210 \text{ N}$$

#8 $t = 8.95 \text{ s}$

$m = 150 \text{ g} = 0.15 \text{ kg}$

$v_i = 25.2 \text{ km/h} = 7 \text{ m/s}$

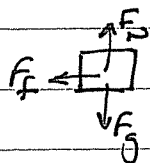
$\Delta d = 32 \text{ m}$

$\mu = 0.080$

(a) $F_g = mg$
 $= 0.15(9.8)$
 $= 1.47 \text{ N}$

(b) $F_f = \mu F_N$
 $= (0.080)(1.47)$
 $= 0.118 \text{ N}$

(c) While puck is travelling towards the goal:



$F_{\text{net}} = F_f$

$= 0.118 \text{ N backwards}$

(d) $\vec{F}_{\text{net}} = m\vec{a}$

$-0.118 = 0.15 \vec{a}$

$\vec{a} = -0.784 \text{ m/s}^2$

(e) $\vec{v}_2 = \vec{v}_1 + \vec{a} \Delta t$

$0 = 7 - 0.784 \Delta t$

$\Delta t = 8.93 \text{ s}$

#9 $m = 55 \text{ g} = 0.055 \text{ kg}$
 $t = 0.0050 \text{ s}$

$\vec{v}_1 = 30 \text{ m/s [E]}$

$\vec{v}_2 = 40 \text{ m/s [W]}$

(a) $\vec{a} = ?$ $\vec{v}_2 = \vec{v}_1 + \vec{a} \Delta t$

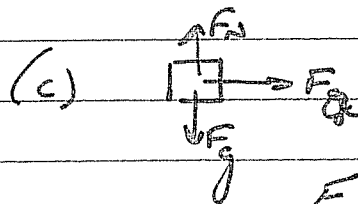
$40 \text{ m/s [W]} = 30 \text{ m/s [E]} + \vec{a}(0.005)$

$40 \text{ m/s [W]} - 30 \text{ m/s [E]} = 0.005 \vec{a}$

$70 \text{ m/s [W]} = 0.005 \vec{a}$

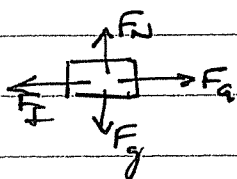
$\vec{a} = 14000 \text{ m/s}^2 \text{ [W]}$

(b) $\vec{F}_{\text{net}} = m\vec{a}$
 $= 0.055(14000)$
 $= 770 \text{ N [W]}$



$F_a = F_{\text{net}} = 770 \text{ N [W]}$

#10 $m = 30 \text{ kg}$
 $F_a = 160 \text{ N}$
 $\mu = ?$



(a) $F_f = F_a = 160 \text{ N}$

(b) $F_f = \mu F_N$
 $160 = \mu (mg)$
 $\mu = 160/294$
 $= 0.544$

#11 $m = 100 \text{ kg}$
 $\vec{v}_1 = 88 \text{ km/h} = 24.44 \text{ m/s}$
 $\Delta d = 100 \text{ m}$
 $\vec{v}_2 = 0 \text{ m/s}$

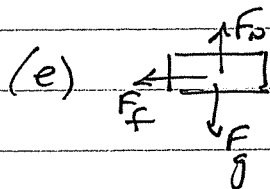
(a) $v = 24.44 \text{ m/s}$

(b) Newton's 1st

(c) $\vec{v}_2^2 = \vec{v}_1^2 + 2a\Delta d$
 $0 = 24.44^2 + 2a(100)$
 $a = -2.99 \text{ m/s}^2$

(d) $\vec{F}_{\text{net}} = m\vec{a}$
 $= 100(-2.99)$
 $= -299 \text{ N}$

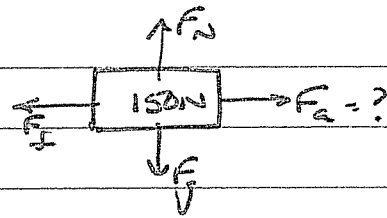
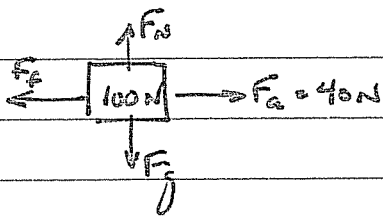
-ve indicates direction



$F_f = F_{\text{net}} = -299 \text{ N}$

(f) $F_f = \mu F_N$
 $299 = \mu mg$
 $299 = \mu (980)$
 $\mu = 0.305$

12



Same surfaces $\therefore \mu$ is same for both

$$\therefore F_{\text{Net}} = 0 \text{ N}$$

$$\therefore F_a = F_f = 40 \text{ N}$$

$$\therefore F_f = \mu_s F_N$$

$$40 = \mu_s (mg)$$

$$40 = \mu_s (100)$$

$$\mu_s = 0.40$$

$$\mu_s = 0.40$$

$$F_f = ?$$

$$F_f = \mu_s F_N$$

$$= 0.40 (150)$$

$$= 60 \text{ N}$$

$$\therefore F_a = 60 \text{ N}$$

$$\therefore F_{\text{Net}} = 0 \text{ N}$$

$$\#13 \quad m = 46 \text{ g} = 0.046 \text{ kg}$$

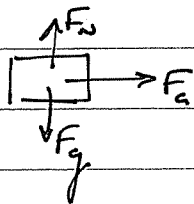
$$\vec{v}_1 = 0 \text{ m/s}$$

$$\vec{v}_2 = 252 \text{ km/h} \approx 70 \text{ m/s}$$

$$\Delta t = 0.005 \text{ s}$$

$$\left. \begin{array}{l} \vec{v}_1 = 0 \text{ m/s} \\ \vec{v}_2 = 252 \text{ km/h} \approx 70 \text{ m/s} \end{array} \right\} \vec{a} = \Delta \vec{v} / \Delta t$$

$$= 14000 \text{ m/s}^2$$



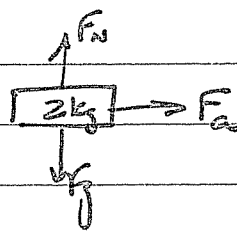
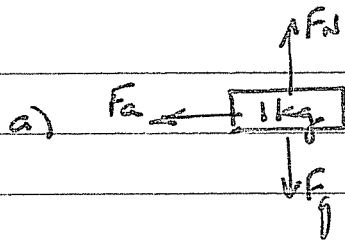
$$F_{\text{Net}} = ma$$

$$F_a = (0.046)(14000)$$

$$= 6440 \text{ N} \leftarrow F_{\text{club on ball}}$$

$$F_{\text{ball on club}} = \text{RxN force} = 6440 \text{ N}$$

#14



$$\left. \begin{array}{l} a = 10 \text{ m/s}^2 \\ m = 2 \text{ kg} \end{array} \right\} \begin{array}{l} \vec{F}_{\text{Net}} = m\vec{a} \\ = 2(10) \\ = 20 \text{ N} \end{array}$$

b) F of 1 kg mass on 2 kg mass $= F_a = F_{\text{Net}} = 20 \text{ N}$

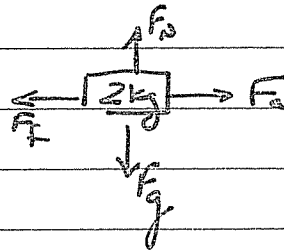
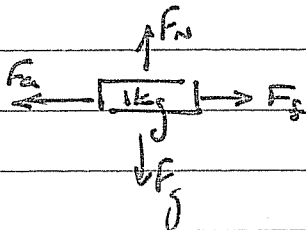
c) F of 2 kg mass on 1 kg mass $= 20 \text{ N}$ (rxn force).

d) $F_{\text{Net}} = ma$

$$20 = 1(a)$$

$$\vec{a} = 20 \text{ m/s}^2 \text{ (backwards)}$$

e) IF FRICTION IS PRESENT



$$\begin{aligned} F_f &= \mu F_N \\ &= 0.05(mg) \\ &= 0.49 \text{ N} \end{aligned}$$

$$\begin{aligned} F_f &= \mu F_N \\ &= 0.05(mg) \\ &= 0.98 \text{ N} \end{aligned}$$

$$F_a = F_{\text{repulsion}} \text{ is still } 20 \text{ N}$$

$$F_a = F_{\text{repulsion}} \text{ is still } 20 \text{ N}$$

$$\begin{aligned} \therefore F_{\text{Net}} &= 20 - 0.49 \\ &= 19.51 \text{ N} \end{aligned}$$

$$\begin{aligned} \therefore F_{\text{Net}} &= 20 - 0.98 \\ &= 19.02 \text{ N} \end{aligned}$$

$$\begin{aligned} \therefore \vec{F}_{\text{Net}} &= m\vec{a} \\ 19.51 &= 1\vec{a} \end{aligned}$$

$$\vec{a} = 19.51 \text{ m/s}^2 \text{ back}$$

$$\begin{aligned} \therefore F_{\text{Net}} &= ma \\ 19.02 &= 2\vec{a} \end{aligned}$$

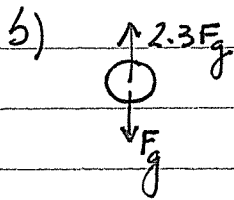
$$\vec{a} = 9.51 \text{ m/s}^2 \text{ forward}$$

#15 Can't do \rightarrow info not given.

#16 a) According to Newton's 3rd Law,

$$F_{\text{ground up on individual}} = 2.3 F_g$$

$$2.3 \times \text{body weight} = 2.3 F_g$$



$$\vec{F}_{\text{Net}} = \Sigma \text{ Forces} = 1.3 F_g \text{ [up]}$$

c) $\vec{v}_1 = 0 \text{ m/s}$

$$\vec{v}_2 = ?$$

$$\Delta t = 0.25 \text{ s}$$

$$\vec{a} =$$

$$\vec{F}_{\text{Net}} = m \vec{a}$$

$$1.3 F_g = m \vec{a}$$

$$1.3 m g = m \vec{a}$$

$$\vec{a} = 1.3 g$$

$$= 12.74 \text{ m/s}^2$$

$$\vec{v}_2 = \vec{v}_1 + \vec{a} t$$

$$= 0 + (12.74)(0.25)$$

$$= 3.185 \text{ m/s}$$

d) Once they are airborne,



$$\therefore \vec{a} = -9.8 \text{ m/s}^2$$

$$\vec{v}_1 = 3.185 \text{ m/s}$$

$$\vec{a} = -9.8 \text{ m/s}^2$$

$$\vec{v}_2 = 0 \text{ m/s}$$

$$\Delta \vec{d} = ?$$

$$\vec{v}_2^2 = \vec{v}_1^2 + 2 \vec{a} \Delta \vec{d}$$

$$0 = (3.185)^2 + 2(-9.8) \Delta \vec{d}$$

$$\Delta \vec{d} = 0.52 \text{ m}$$